



STDP in adaptive neurons gives close-to-optimal information transmission

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Spike-frequency adaptation is known to enhance the transmission of information in sensory spiking neurons by rescaling the dynamic range for input processing, matching it to the temporal statistics of the sensory stimulus. Achieving maximal information transmission has also been recently postulated as a role for spike-timing-dependent plasticity (STDP). However, the link between optimal plasticity and STDP in cortex remains loose, as does the relationship between STDP and adaptation processes. We investigate how STDP, as described by recent minimal models derived from experimental data, influences the quality of information transmission in an adapting neuron. We show that a phenomenological model based on triplets of spikes yields almost the same information rate as an optimal model specially designed to this end. In contrast, the standard pair-based model of STDP does not improve information transmission as much. This result holds not only for additive STDP with hard weight bounds, known to produce bimodal distributions of synaptic weights, but also for weight-dependent STDP in the context of unimodal but skewed weight distributions. We analyze the similarities between the triplet model and the optimal learning rule, and find that the triplet effect is an important feature of the optimal model when the neuron is adaptive. If STDP is optimized for information transmission, it must take into account the dynamical properties of the postsynaptic cell, which might explain the target-cell specificity of STDP. In particular, it accounts for the differences found *in vitro* between STDP at excitatory synapses onto principal cells and those onto fast-spiking interneurons.

Keywords: STDP, plasticity, spike-frequency adaptation, information theory, optimality

INTRODUCTION

The experimental discovery of spike-timing-dependent plasticity (STDP) in the mid-nineties (Bell et al., 1997; Magee and Johnston, 1997; Markram et al., 1997; Bi and Poo, 1998; Zhang et al., 1998) led to two questions, in particular. The first is: what is the simplest way of describing this complex phenomenon? This question has been answered in a couple of minimal models (phenomenological approach) whereby long-term potentiation (LTP) and long-term depression (LTD) are reduced to the behavior of a small number of variables (Gerstner et al., 1996; Kempter et al., 1999; Song et al., 2000; van Rossum et al., 2000; Rubin et al., 2001; Gerstner and Kistler, 2002a; Froemke et al., 2006; Pfister and Gerstner, 2006; Clopath et al., 2010; see Morrison et al., 2008 for a review). Because they are inspired by *in vitro* plasticity experiments, the state variables usually depend solely on what is experimentally controlled, i.e., on spike times and possibly on the postsynaptic membrane potential. They are computationally cheap enough to be used in large-scale simulations (Morrison et al., 2007; Izhikevich and Edelman, 2008). The second question has to do with the functional role of STDP: what is STDP good for? The minimal models mentioned above can address this question only indirectly, by solving the dynamical equation of synaptic plasticity for input with given stationary properties (Kempter et al., 1999; van Rossum et al., 2000; Rubin et al., 2001). An alternative approach is to postulate a role for synaptic plasticity, and formulate it in the mathematical framework of optimization (“top-down approach”). Thus, in artificial neural networks,

Hebbian-like learning rules were shown to arise from unsupervised learning paradigms such as principal components analysis (Oja, 1982, 1989), independent components analysis (ICA; Intrator and Cooper, 1992; Bell and Sejnowski, 1995; Clopath et al., 2008), maximization of mutual information (MI; Linsker, 1989), sparse coding (Olshausen and Field, 1996; Smith and Lewicki, 2006), and predictive coding (Rao and Ballard, 1999). In spiking neurons, local STDP-like learning rules were obtained from optimization criteria such as maximization of information transmission (Chechik, 2003; Toyozumi et al., 2005, 2007), information bottleneck (Klampf et al., 2009), maximization of the neuron’s sensitivity to the input (Bell and Parra, 2005), reduction of the conditional entropy (Bohte and Mozer, 2007), slow-feature analysis (Sprekeler et al., 2007), and maximization of the expected reward (Xie and Seung, 2004; Pfister et al., 2006; Florian, 2007; Sprekeler et al., 2009).

The functional consequences of STDP have mainly been investigated in simple integrate-and-fire neurons, where the range of temporal dependencies in the postsynaptic spike train spans no more than the membrane time constant. Few studies have addressed the question of the synergy between STDP and more complex dynamical properties on different timescales. In Seung (2003), more complex dynamics were introduced not at the cell level, but through short-term plasticity of the synapses. The postsynaptic neuron was then able to become selective to temporal order in the input. Another elegant approach to this question was taken in Lengyel et al. (2005) in a model of hippocampal autoassociative memory. Memories were

encoded in the phase of firing of a population of neurons relative to an ongoing theta oscillation. Under the assumption that memories are stored using a classical form of STDP, they derived the form of the postsynaptic dynamics that would optimally achieve their recall. This turned out to match what they recorded *in vitro*, suggesting that STDP might optimally interact with the dynamical properties of the postsynaptic cell in this memory storage task.

More generally, optimality models are ideally suited to study plasticity and dynamics together. Indeed, optimal learning rules contain an explicit reference to the dynamical properties of the postsynaptic cell, by means of the transfer function that maps input to output values. This function usually appears in the formulation of a gradient ascent on the objective function. In this article, we exploit this in order to relate STDP to spike-frequency adaptation (SFA), an important feature of the dynamics of a number of cell types found in cortex. Recent phenomenological models of STDP have emphasized the importance of the interaction between postsynaptic spikes in the LTP process (Senn et al., 2001; Pfister and Gerstner, 2006; Clopath et al., 2010). In these models, the amount of LTP obtained from a pre-before-post spike pair increases with the number of postsynaptic spikes fired in the recent past, which we call the “triplet effect” (combination of one pre-spike and at least two post-spikes). The timescale of this post–post interaction was fitted to *in vitro* STDP experiments, and found to be very close to that of adaptation (100–150 ms).

We reason that STDP may be ideally tuned to SFA of the postsynaptic cell. We specifically study this idea within the framework of optimal information transmission (infomax) between input and output spike trains. We compare the performance of a learning rule derived from the infomax principle in Toyozumi et al. (2005), to that of the triplet model developed in Pfister and Gerstner (2006). We also compare them to the standard pair-based learning window used in most STDP papers. Performance is measured in terms of information theoretic quantities. We find that the triplet learning rule yields a better performance than pair-STDP on a spatio-temporal receptive field formation task, and that this advantage crucially depends on the presence of postsynaptic SFA. This reflects a synergy between the triplet effect and adaptation. The reasons for this optimality are further studied by showing that the optimal model features a similar triplet effect when the postsynaptic neuron adapts. We also show that both the optimal and triplet learning rules increase the variability of the postsynaptic spike trains, and enlarge the frequency band in which signals are transmitted, extending it toward lower frequencies (1–5 Hz). Finally, we exploit the optimal model to predict the form of the STDP mechanism for two different target cell types. The results qualitatively agree with the *in vitro* data reported for excitatory synapses onto principal cells and those onto fast-spiking (FS) inhibitory interneurons. In the model, the learning windows are different because the intrinsic dynamical properties of the two postsynaptic cell types are different. This might be the functional reason for the target-cell specificity of STDP.

MATERIALS AND METHODS

NEURON MODEL

We simulate a single stochastic point neuron (Gerstner and Kistler, 2002b) and a small portion of its incoming synapses ($N = 1$ for the simulation of *in vitro* experiments, $N = 100$ in the rest of the paper). Each postsynaptic potential (PSP) adds up linearly to form the total modeled synaptic drive

$$u(t) = \sum_{j=1}^N w_j \varepsilon_j(t) \quad (1)$$

with

$$\varepsilon_j(t) = \int_0^t x_j(t') \exp\left(-\frac{t-t'}{\tau_m}\right) dt' \quad (2)$$

where $x_j(t) = \sum_{t_j^f} \delta(t - t_j^f)$ denotes the j^{th} input spike train, and w_j (mV) are the synaptic weights. The effect of thousands of other synapses is not modeled explicitly, but treated as background noise. The firing activity of the neuron is entirely described by an instantaneous firing density

$$\rho(t) = g[u(t)]M(t) \quad (3)$$

where

$$g[u] = g_0 + r_0 \log\left[1 + \exp(\beta(u - u_T))\right] \quad (4)$$

is the gain function, drawn in **Figure 1A**. Refractoriness and SFA both modulate the instantaneous firing rate via

$$M(t) = \exp[-(g_R(t) + g_A(t))] \quad (5)$$

The variables g_R and g_A evolve according to

$$\frac{dg_R}{dt} = -\frac{g_R(t)}{\tau_R} + q_R \gamma(t) \quad \text{and} \quad \frac{dg_A}{dt} = -\frac{g_A(t)}{\tau_A} + q_A \gamma(t) \quad (6)$$

where $\gamma(t) = \sum_{t_{\text{post}}^f} \delta(t - t_{\text{post}}^f)$ is the postsynaptic spike train and $0 < \tau_R \ll \tau_A$ are the time constants of refractoriness and adaptation respectively. The firing rate thus becomes a compressive function of the average gain, as shown in **Figure 1B**. The response of the neuron to a step in input firing rate is depicted in **Figure 1C**.

For the simulation of *in vitro* STDP experiments, only one synapse is investigated. The potential u is thus given a baseline u_b (to which the PSP of the single synapse will add) such that $g(u_b)$ yields a spontaneous firing rate of 7.5 Hz (**Figure 1B**).

In some of our simulations, postsynaptic SFA is switched off ($q_A = 0$). In order to preserve the same average firing rate given the same synaptic weights, r_0 is rescaled accordingly (**Figures 1A,B**, dashed lines).

In the simulation of **Figure 8**, we add a third variable g_B in the after-spike kernel M in order to model a FS inhibitory interneuron. This variable jumps down ($q_B < 0$) following every postsynaptic spike, and decays exponentially with time constant τ_B (with $\tau_R \ll \tau_B < \tau_A$).

All simulations were written in Objective Caml and run on a standard desktop computer operated by Linux. We used simple Euler integration of all differential equations, with 1 ms time resolution (0.1 ms for the simulation of *in vitro* experiments). All parameters are listed in **Table 1** together with their values.

PRESYNAPTIC FIRING STATISTICS

To analyze the evolution of information transmission under different plasticity learning rules, we consider $N = 100$ periodic input spike of 5 s duration generated once and for all (see below). This “frozen noise” is then replayed continuously, feeding the postsynaptic neuron for as long as is necessary (e.g., for learning, or for MI estimation).

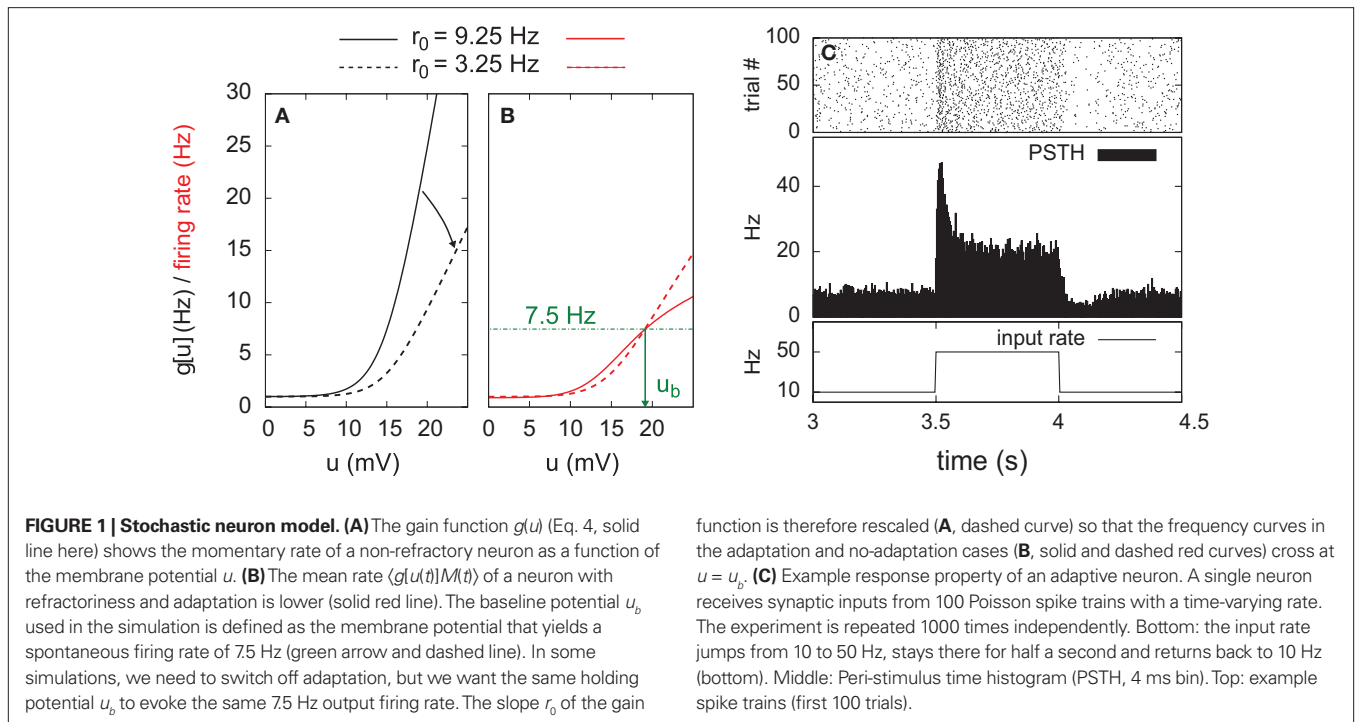


Table 1 | Baseline values of all parameters defined in the text.

Neuron model		Optimal rule		Triplet rule		Pair rule		Weight bounds	
τ_m	20 ms	η_o	0.04	η_3	1.0	η_2	1.0	w_{min}	0 mV
g_0	1 Hz (35)	τ_c	20 ms	τ_+	16.8 ms	τ_+	16.8 ms	w_{max}	4 mV
r_0	9.25 Hz (3.25)	τ_g	10 s	τ_-	33.7 ms	τ_-	33.7 ms	a	9
β	0.5 mV ⁻¹	γ	1 (0)	τ_y	114 ms				
u_T	15 mV	g_{targ}	<i>ad hoc</i>	\tilde{A}_2^-	2.8×10 ⁻³	\tilde{A}_2^-	2.8×10 ⁻³		
τ_R	2 ms	λ	0.0094	A_3^+	6.5×10 ⁻³	A_2^+	5.6×10 ⁻³		
τ_A	150 ms			ρ_{targ}	<i>ad hoc</i>	ρ_{targ}	<i>ad hoc</i>		
q_R	100			τ_p	10 s	τ_p	10 s		
q_A	1 (0)								

Some parameters were set to different values when the neuron was non-adapting (italic numbers). Similarly, some parameters were different for the simulations of in vitro experiment (bold faces).

To generate the time-varying rates of the N processes underlying this frozen noise, we first draw point events at a constant Poisson rate of 10 Hz, and then smooth them with a Gaussian kernel of width 150 ms. Rates are further multiplicatively normalized so that each presynaptic neuron fires an average of 10 spikes per second. We emphasize that this process describes the statistics of the inputs *across different learning experiments*. When we mention “independent trials,” we mean a set of experiments which have their own independent realizations of those input spike trains. However, in one learning experiment, a single such set of N input spike trains is chosen and replayed continuously as input to the postsynaptic neuron. The input is therefore deterministic and periodic. When the periodic input is generated, some neurons can happen to fire at some point during those 5 s within a few milliseconds of each other, and by virtue of the periodicity, these

synchronous firing events will repeat in each period, giving rise to strong spatio-temporal correlations in the inputs. We are interested in seeing how different learning rules can exploit this correlational structure to improve the information carried by the postsynaptic activity about those presynaptic spike trains. We now describe what we mean by information transmission under this specific stimulation scenario.

INFORMATION THEORETIC MEASUREMENTS

The neuron can be seen as a noisy communication channel in which multidimensional signals are compressed and distorted before being transmitted to subsequent receivers. The goodness of a communication channel is traditionally measured by Shannon’s MI between the input and output variables, where the input is chosen randomly from some “alphabet” or vocabulary of symbols.

Here, the input is deterministic and periodic (**Figure 2A**). We therefore define the quality of information transmission by the reduction of uncertainty about the phase of the current input if we observe a certain output spike train at an unknown time. In discrete time (with time bin $\Delta = 1$ ms), there are only $N_\phi = 5000$ possible phases since the input has a period of 5 s. Therefore, the maximum number of bits that the noisy postsynaptic neuron can transmit is $\log_2(N_\phi) \simeq 12.3$ bits. We further assume that an observer of the output neuron can only see “words” corresponding to spike trains of finite duration $T = K\Delta$. We assume $T = 1$ s for most of the paper, which corresponds to $K = 1000$ time bins. This choice is justified below.

The discretized output spike trains of size K (binary vectors), called Y^K , can be observed at random times and play the role of the output variable. The input random variable is the phase ϕ of the input. The quality of information transmission is quantified by the MI, i.e., the difference between the total response entropy $H(Y^K) = \langle \log_2 P(Y^K) \rangle_{Y^K}$ and the noise entropy $H(Y^K | \phi) = \langle \langle \log_2 P(Y^K | \phi) \rangle_{Y^K | \phi} \rangle_\phi$. Here $\langle \cdot \rangle$ denotes the ensemble average. In order to compute these entropies, we need to be able to estimate the probability of occurrence of any sample word Y^K , knowing and not knowing the phase. To do so, a large amount of data is first generated. The noisy neuron is fed continuously for a large number of periods $N_p = 100$ with a single periodic set of input spike trains and a fixed set of synaptic weights. The output spikes are recorded with $\Delta = 1$ ms precision. From this very long output spike train, we randomly pick words of length K and gather them in a set \mathcal{S} . We take $|\mathcal{S}| = 1000$. This is our sample data.

In general, estimating the probability of a random binary vector of size K is very difficult if K is large. Luckily, we have a statistical model for how spike trains are generated (Eq. 3), which considerably reduces the amount of data needed to produce a good estimate. Specifically, if the refractory state of the neuron $[g_R(t), g_A(t)]$ is known at time t (initial conditions), then the probability $1 - \exp(-\rho_k \Delta) \simeq \rho_k \Delta$ of the postsynaptic neuron spiking is also known for each of the K time bins following t (Eqs 3–5). The

neuron model gives us the probability that a word Y^K occurred at time t – not necessarily the time at which the word was actually picked – (Toyoizumi et al., 2005):

$$P(Y^K | t, g_R(t), g_A(t)) = \exp \left[\sum_{k=1}^K Y_k^K \log(\rho_k \Delta) + (1 - Y_k^K) \log(1 - \rho_k \Delta) \right] \quad (7)$$

where $\rho_k = \rho(t + k\Delta)$ and Y_k^K is one if there is a spike in the word at position k , and 0 otherwise. To compute the conditional probability of occurrence of a word Y^K knowing the phase ϕ , we have to further average Eq. 7:

$$P(Y^K | \phi) = \langle P(Y^K | t) \rangle_{t \text{ with } \Phi(t) = \phi} \quad (8)$$

where $\Phi(t) = 1 + (t \bmod N_\phi)$ denotes the phase at time t . Averaging over multiple times with same phase also averages over the initial conditions $[g_R(t), g_A(t)]$, so that they do not appear in Eq. 8. The average in Eq. 8 is estimated using a set of 10 randomly chosen times t_i with $\Phi(t_i) = \phi$.

The full probability of observing a word Y^K is given by $P(Y^K) = 1/N_\phi \sum_{\phi=1}^{N_\phi} P(Y^K | \phi)$ where $P(Y^K | \phi)$ is computed as described above. Owing to the knowledge of the model that underlies spike generation, and to this huge averaging over all the possible phases, the obtained $P(Y^K)$ is a very good estimate of the true density. We can then take a Monte-Carlo approach to estimate the entropies, using the set \mathcal{S} of randomly picked words: $H(Y^K) = -\sum_{Y^K} P(Y^K) \log_2 P(Y^K)$ can be estimated by

$$\hat{H}(Y^K) = -\frac{1}{|\mathcal{S}|} \sum_{Y^K \in \mathcal{S}} \log_2 P(Y^K) \quad (9)$$

and $H(Y^K | \phi) = -\sum_{\phi} P(\phi) \sum_{Y^K} P(Y^K) \frac{P(Y^K | \phi)}{P(Y^K)} \log_2 P(Y^K | \phi)$ is estimated using

$$\hat{H}(Y^K | \phi) = -\frac{1}{N_\phi} \sum_{\phi=1}^{N_\phi} \frac{1}{|\mathcal{S}|} \sum_{Y^K \in \mathcal{S}} \frac{P(Y^K | \phi)}{P(Y^K)} \log_2 P(Y^K | \phi) \quad (10)$$

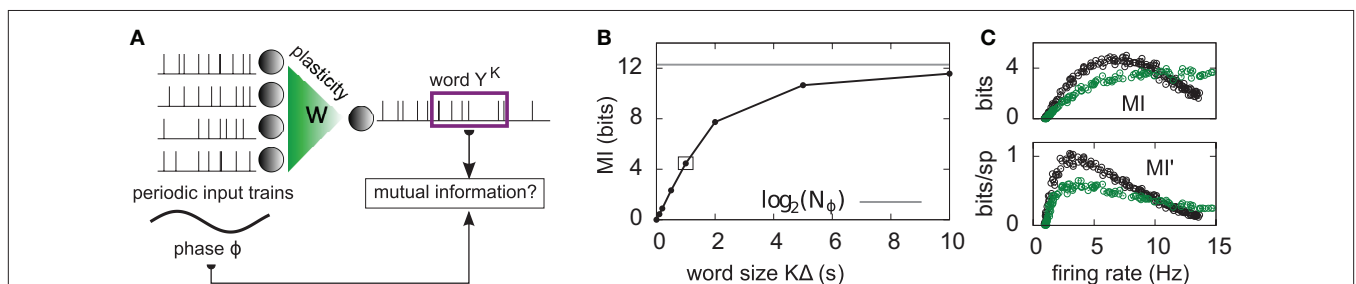


FIGURE 2 | Information transmission through a noisy postsynaptic neuron. (A) Schematic representation of the feed-forward network. Five-second input spike trains repeat continuously in time (periodic input) and drive a noisy and possibly adapting output neuron via plastic synapses. It is assumed that an observer of the output spike train has access to portions Y^K of it, called “words,” of duration $T = K\Delta$. The observer does not have access to a clock, and therefore has a flat prior expectation over possible phases before observing a word. The goodness of the system, given a set of synaptic weights \mathbf{w} , is measured by the reduction of uncertainty about the phase, gained from the observation of an output word Y^K (mutual information, see text). (B) For a random set of synaptic

weights (20 weights at 4 mV, the rest at 0), the mutual information (MI) is reported as a function of the output word size $K\Delta$. Asymptotically, the MI converges to the theoretical limit given by $\log_2(N_\phi)$ (12.3 bits). In the rest of this study, 1-s output words are considered (square). (C) Mutual information (MI, top) and information per spike (MI', bottom) as a function of the average firing rate. Black: with SFA. Green: without SFA. Each dot is obtained by setting a fraction of randomly chosen synaptic efficacies to the upper bound (4 mV) and the rest to 0. The higher the fraction of non-zero weights, the higher the firing rate. The information per spike is a relevant quantity because spike generation costs energy.

The MI estimate is the difference of these two entropies, and is expressed in bits. In **Figure 2C**, we introduce the information per spike MI' (bits/spike), obtained by dividing the MI by the expected number of spikes in a window of duration $K\Delta$. **Figure 2B** shows that the MI approaches its upper bound $\log_2(N_\phi)$ as the word size increases. The word size considered here (1 s) is large enough to capture the effects of SFA while being small enough not to saturate the bound.

Although we constrain the postsynaptic firing rate to lie around a fixed value ρ_{targ} (see homeostasis in the next section), the rate will always jitter. Even a small jitter of less than 0.5 Hz (which we have in the present case) makes it impossible to directly compare entropies across learning rules. Indeed, while the MI depends only weakly on small deviations of the firing rate around ρ_{targ} , the response and noise entropies have much larger (co-) variations. In order to compare the entropies across learning rules, we need to know what the entropy would have been if the rate was exactly ρ_{targ} instead of $\rho_{\text{targ}} + \epsilon$. We therefore compute the entropy $[H(\mathbf{Y}^K) \text{ or } H(\mathbf{Y}^K|\phi)]$ for different firing rates in the vicinity of ρ_{targ} . These firing rates are achieved by slightly rescaling the synaptic weights, i.e., $w_{ij} \leftarrow \kappa w_{ij}$ where κ takes several values around 1. We then fit a linear model $H = a\rho + b$, and evaluate H at ρ_{targ} .

The computation of the conditional probabilities $P(\mathbf{Y}^K|\phi)$ was accelerated on an ATI Radeon (HD 4850) graphics processing unit (GPU), which was 130 times faster than a decent CPU implementation.

LEARNING RULES

Optimal learning rule

The optimal learning rule aims at maximizing information transmission under some metabolic constraints (“infomax” principle). Toyozumi et al. (2005, 2007) showed that this can be achieved by means of a stochastic gradient ascent on the following objective function

$$\mathbb{L} = \mathbb{I} - \gamma \mathbb{D} - \lambda \Psi \tag{11}$$

whereby the mutual information \mathbb{I} between input and output spike trains competes with a homeostatic constraint on the mean firing rate \mathbb{D} and a metabolic penalty Ψ for strong weights that are often active. The first constraint is formulated as $\mathbb{D} = \text{KL}[P(\mathbf{Y}^K), \tilde{P}(\mathbf{Y}^K)]$ where KL denotes the Kullback–Leibler (KL) divergence. P denotes the true probability distribution of output spike trains produced by the stochastic neuron model, while \tilde{P} assumes a similar model in which the gain $g(t)$ is kept constant at a target gain g_{targ} . Minimizing the divergence between P and \tilde{P} therefore means driving the average gain close to g_{targ} , thus implementing firing rate homeostasis. The second constraint reads $\Psi = \sum_j w_j \langle n_j \rangle_{\mathbf{x}^k}$, whereby the cost for synapse j is proportional to its weight w_j and to the average number n_j of presynaptic spikes relayed during the K time bins under consideration. The Lagrange multipliers γ and λ set the relative importance of the three objectives.

Performing gradient ascent on \mathbb{L} yields the following online learning rule (Toyozumi et al., 2005, 2007):

$$\frac{dw_j}{dt} = \eta_o [C_j(t)B_{\text{post}}(t) - \lambda x_j(t)] \tag{12}$$

where

$$C_j(t) = \int_0^t dt' \exp\left(-\frac{t-t'}{\tau_c}\right) \epsilon_j(t') \frac{g'[u(t')]}{g[u(t')]} [y(t') - g[u(t')]] M(t') \tag{13}$$

and

$$B_{\text{post}}(t) = y(t) \log \left[\frac{g[u(t)]}{\bar{g}} \left(\frac{g_{\text{targ}}}{\bar{g}} \right)^\gamma \right] - M(t) [g[u(t)] - \bar{g} + \gamma(g_{\text{targ}} - \bar{g})] \tag{14}$$

η_o is a small learning rate. The first term C_j is Hebbian in the sense that it reflects the correlations between the input and output spike trains. B_{post} is purely postsynaptic: it compares the instantaneous gain g to its average \bar{g} (information term), as well as the average gain to its target value g_{targ} (homeostasis). The average \bar{g} is estimated online by a low pass filter of g with time constant τ_g . The time course of these quantities is shown in **Figure 3A** for example spike trains of 1 s duration, for $\gamma = 0$.

Because of the competition between the three objectives in Eq. 11, the homeostatic constraint does not yield the exact desired gain g_{targ} . In practice, we set the value of g_{targ} empirically, such that the actual mean firing rate approaches the desired value.

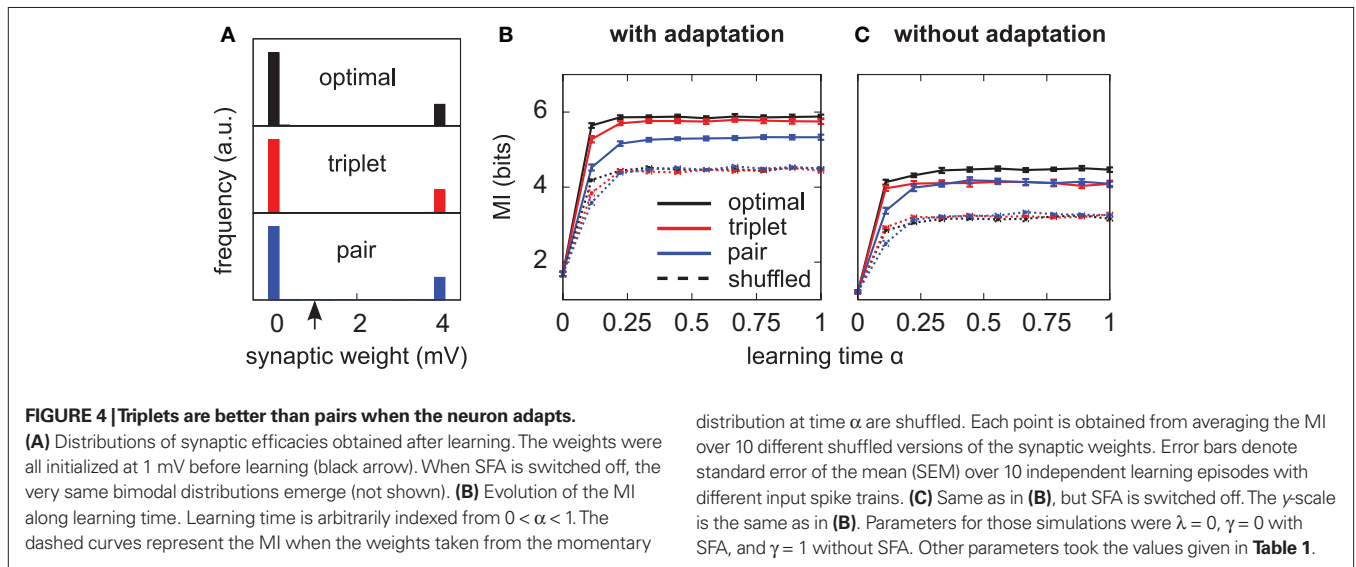
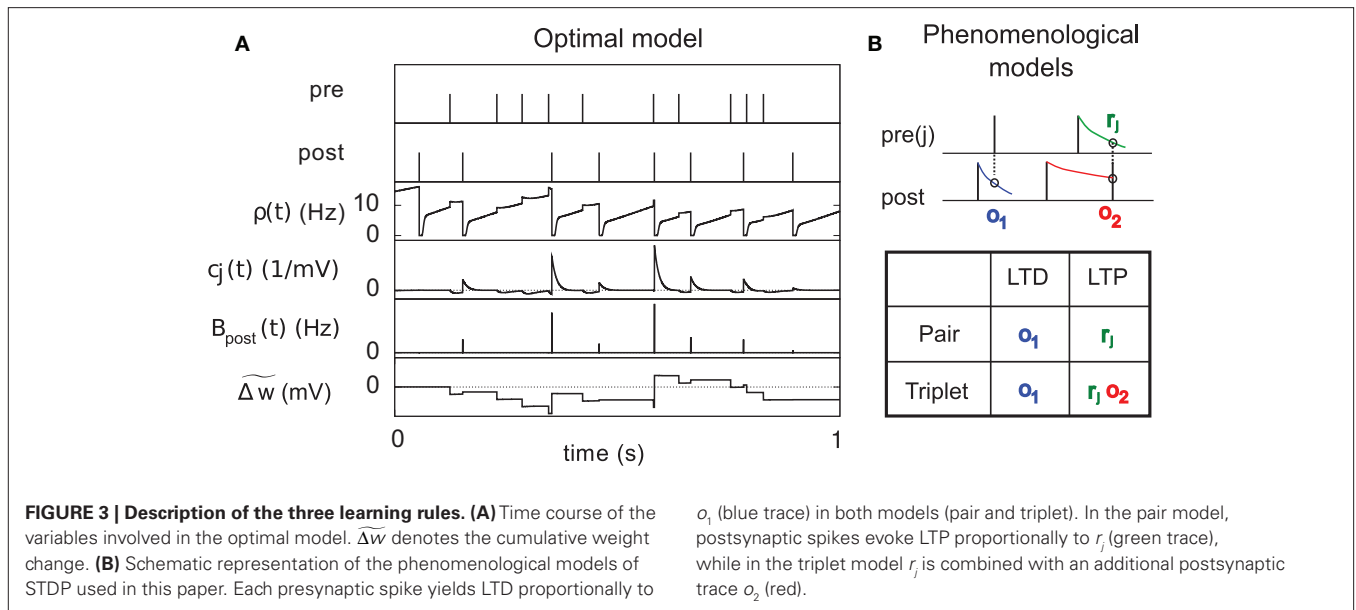
Finally, we use τ_c , η_o , and λ as three free parameters to fit the results of *in vitro* STDP pairing experiments (**Figure 8**). τ_c is set empirically equal to the membrane time constant $\tau_m = 20$ ms, while η_o and λ are determined through a least-squares fit of the experimental data. The learning rate η_o can be rescaled arbitrarily. In the simulations of receptive-field development (**Figures 4–6**), λ is set to 0 so as not to perturb unnecessarily the prime objective of maximizing information transmission. It is also possible to remove the homeostasis constraint ($\gamma = 0$) in the presence of SFA. As can be seen in **Figure 2C**, the MI has a maximum at 7.5 Hz when the neuron adapts, so that firing rate control comes for free in the information maximization objective. We therefore set $\gamma = 0$ when the neuron adapts, and $\gamma = 1$ when it does not. In fact, the homeostasis constraint only slightly impairs the infomax objective: we have checked that the MI reached after learning (**Figures 4 and 5**) does not vary by more than 0.1 bit when γ takes values as large as 20.

Triplet-based learning rule

We use the minimal model developed in Pfister and Gerstner (2006) with “all-to-all” spike interactions. Presynaptic spikes at synapse j leave a trace r_j (**Figure 3B**) which jumps by 1 after each spike and otherwise decays exponentially with time constant τ_+ . Similarly, the postsynaptic spikes leave two traces, o_1 and o_2 , which jump by 1 after each postsynaptic spike and decay exponentially with time constants τ_- and τ_y respectively:

$$\frac{dr_j}{dt} = -\frac{r_j}{\tau_+} + x_j(t) \quad \frac{do_1}{dt} = -\frac{o_1}{\tau_-} + y(t) \quad \frac{do_2}{dt} = -\frac{o_2}{\tau_y} + y(t) \tag{15}$$

where $x_j(t)$ and $y(t)$ are sums of δ -functions at each firing time as introduced above. The synaptic weight w_j undergoes LTD proportionally to o_1 after each presynaptic spike, and LTP proportionally to $r_j o_2$ following each postsynaptic spike:



$$\frac{dw_j}{dt} = \eta_3 \left[A_3^+ r_j(t) o_2(t - \epsilon) y(t) - A_2^- a_1(t) x_j(t) \right] \quad (16)$$

where η_3 denotes the learning rate. Note that o_2 is taken just before its update. Under the assumption that pre- and postsynaptic spike trains are independent Poisson processes with rates ρ_x and ρ_y respectively, the average weight change was shown in Pfister and Gerstner (2006) to be proportional to

$$\langle \Delta w \rangle \propto \rho_x \rho_y \left(\rho_y - \frac{\tau_- A_2^-}{\tau_+ \tau_y A_3^+} \right) \quad (17)$$

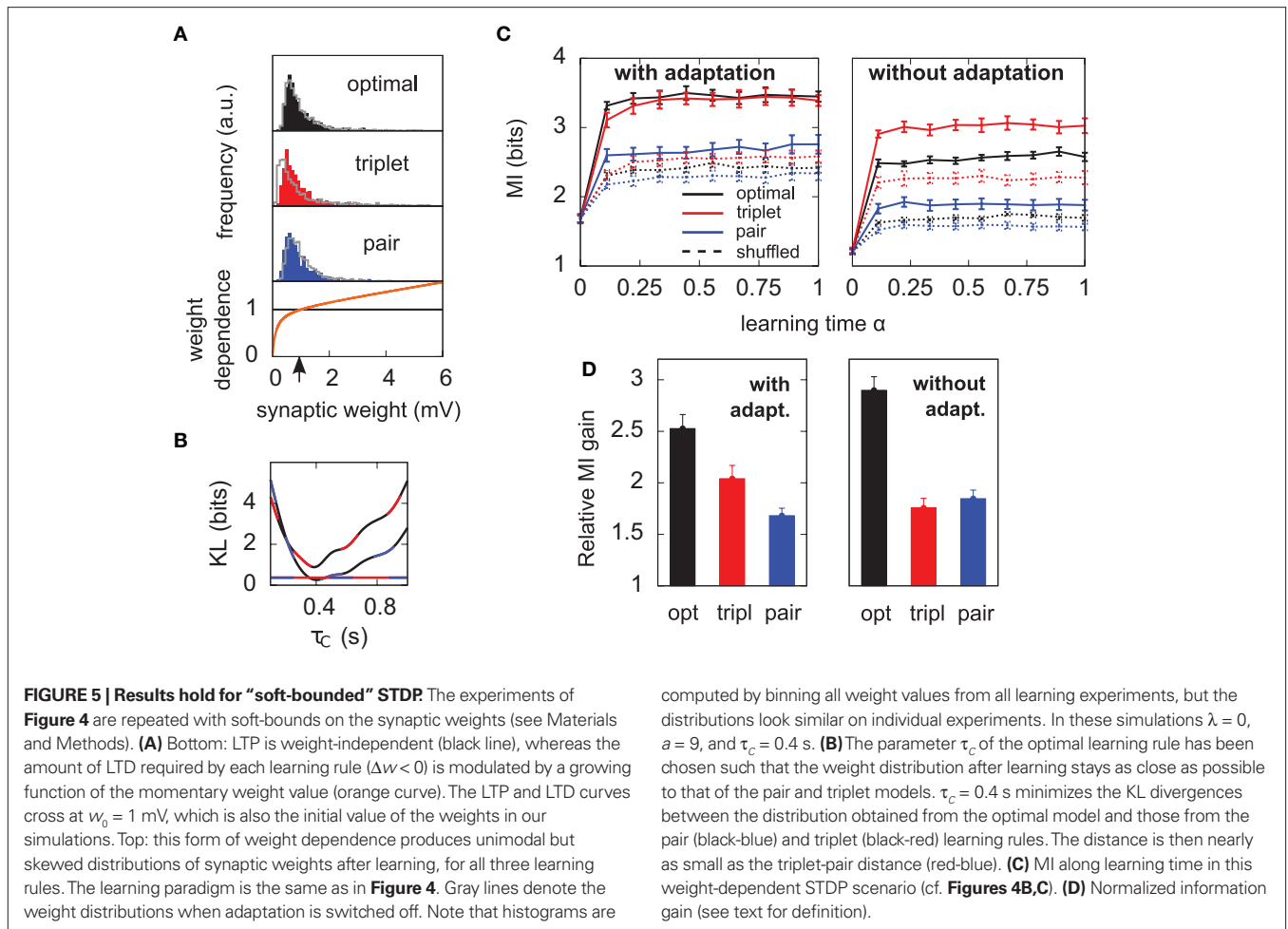
The rule is thus structurally similar to a Bienenstock–Cooper–Munro (BCM) learning rule (Bienenstock et al., 1982) since it is linear in the presynaptic firing rates and non-linear in the postsynaptic rate. It is possible to roughly stabilize the postsynaptic firing rate at a target value ρ_{targ} , by having A_2^- slide in an activity-dependent manner:

$$A_2^-(t) = \tilde{A}_2^- \frac{\bar{\rho}^3(t)}{\rho_{\text{targ}}^3} \quad (18)$$

where \tilde{A}_2^- is a starting value and $\bar{\rho}$ is an average of the instantaneous firing rate on the timescale of seconds or minutes (time constant τ_p). Finally, A_3^+ is set to make ρ_{targ} an initial fixed point of the dynamics in Eq. 17:

$$A_3^+ = \frac{\tau_- \tilde{A}_2^-}{\rho_{\text{targ}} \tau_+ \tau_y} \quad (19)$$

The postsynaptic rate should therefore roughly remain equal to its starting value ρ_{targ} . In practice, the Poisson assumption is not valid because of adaptation and refractoriness, and independence becomes violated as learning operates. This causes the postsynaptic firing rate to deviate and stabilize slightly away from the target ρ_{targ} . We therefore always set ρ_{targ} empirically so that the firing rate stabilizes to the true desired target.



Pair-based learning rule

We use a pair-based STDP rule structurally similar to the triplet rule described by Eq. 16 (**Figure 3B**). The mechanism for LTD is identical, but LTP does not take into account previous postsynaptic firing:

$$\frac{dw_j}{dt} = \eta_2 \left[A_2^+ r_j(t) y(t) - A_2^- a_1(t) x_j(t) \right] \quad (20)$$

where η_2 is the learning rate. A_2^- also slides in an activity-dependent manner according to Eq. 18, to help stabilizing the output firing rate at a target ρ_{target} . A_2^+ is set such that LTD initially balances LTP, i.e.,

$$A_2^+ = \frac{\tilde{A}_2^- \tau_c}{\tau_+} \quad (21)$$

Comparing learning rules in a fair way requires making sure that their learning rates are equivalent. Since the two rules share the same LTD mechanism, we can simply take the same value for \tilde{A}_2^- as well as $\eta_2 = \eta_3$. Since LTD is dynamically regulated to balance LTP on average in both rules, this ensures that they also share the same LTP rate.

Weight bounds

In order to prevent the weights from becoming negative or from growing too large, we set hard bounds on the synaptic efficacies for all three learning rules, when not stated otherwise. That is, if the learning rule requires a weight change Δw_j , w_j is set to

$$w_j \leftarrow \min \left[w_{\text{max}}, \max \left(0, w_j + \Delta w_j \right) \right] \quad (22)$$

This type of bounds, in which the weight change is independent of the initial synaptic weight itself, is known to yield bimodal distributions of synaptic efficacies. In the simulation of **Figure 5**, we also consider the following soft bounds to extend the validity of our results to unimodal distributions of weights:

$$\begin{aligned} \text{if } \Delta w_j \geq 0 \quad & \text{then } w_j \leftarrow w_j + \Delta w_j \\ \text{if } \Delta w_j < 0 \quad & \text{then } w_j \leftarrow w_j + \left[1 - \frac{1}{1 + a \frac{w_j}{w_0}} + \left(\frac{1}{1 + a} \right) \frac{w_j}{w_0} \right] \Delta w_j \end{aligned} \quad (23)$$

where a is a free parameter and $w_0 = 1$ mV is the value at which synaptic weights are initialized at the beginning of all learning experiments. This choice of soft-bounds is further motivated in Section “Results.” The shapes of the LTP and LTD weight-dependent factors are drawn in **Figure 5A**, for $a = 9$. Note that the LTD and LTP factors cross at w_0 , which ensures that the balance between LTP and LTD set by Eqs 19 and 21 is initially preserved.

When the soft-bounds are used, the parameter τ_c of the optimal model is adjusted so that the weight distribution obtained with the optimal rule best matches the weight distributions of the

pair and triplet rules. This parameter indeed has an impact on the spread of the weight distribution: the optimal model knows about the generative model that underlies postsynaptic spike generation, and therefore takes optimally the noise into account, as long as τ_c spans no more than the width of the postsynaptic autocorrelation Toyoizumi et al. (2005). If τ_c is equal to this width (about 20 ms), some weights can grow very large (>50 mV), which results in non-realistic weight distributions. Increasing τ_c imposes more detrimental noise such that all weights are kept within reasonable bounds. In order to constrain τ_c in a non-arbitrary way, we ran the learning experiment for several values of τ_c and computed the KL divergences between weight distributions (optimal-triplet, optimal-pair). τ_c is chosen to minimize these, as shown in **Figure 5B**.

SIMULATION OF *IN VITRO* EXPERIMENTS

To obtain the predictions of the optimal model on standard *in vitro* STDP experiments, we compute the weight change of a single synapse ($N = 1$) according to Eq. 12. The effect of the remaining thousands of synapses is concentrated in a large background noise, obtained by adding a $u_b = 19$ mV baseline to the voltage. The gain becomes $g_b = g(u_b) \simeq (21.45$ Hz, which in combination with adaptation and refractoriness would yield a spontaneous firing rate of about 7.5 Hz (see **Figure 1**). Spontaneous firing is artificially blocked, however. Instead, the neuron is forced to fire at precise times as described below.

The standard pairing protocol is made of a series of pre–post spike pairs, the spikes within the same pair being separated by $\Delta s = t_{\text{post}} - t_{\text{pre}}$. Pairs are repeated with some frequency f . The average \bar{g} is taken fixed and equal to g_b , considering that STDP is optimal for *in vivo* conditions such that \bar{g} should not adapt to the statistics of *in vitro* conditions. The homeostasis is turned off ($\gamma = 0$) in order to consider only the effects of the infomax principle.

RESULTS

We study information transmission through a neuron modeled as a noisy communication channel. It receives input spike trains from a hundred plastic excitatory synapses, and stochastically generates output spikes according to an instantaneous firing rate modulated by presynaptic activities. Importantly, the firing rate is also modulated by the neuron's own firing history, in a way that captures the SFA mechanism found in a large number of cortical cell types. We investigate the ability of three different learning rules to enhance information transmission in this framework. The first learning rule is the standard pair-based STDP model, whereby every single pre-before-post (resp. post-before-pre) spike pair yields LTP (resp. LTD) according to a standard double exponential asymmetric window (Bi and Poo, 1998; Song et al., 2000). The second one was developed in Pfister and Gerstner (2006) and is based on triplets of spikes. LTD is obtained similarly to the pair rule, whereas LTP is obtained from pairing a presynaptic spike with two postsynaptic spikes. The third learning rule (Toyoizumi et al., 2005) is derived from the infomax principle, under some metabolic constraints.

TRIPLET-STDP IS BETTER THAN PAIR-STDP WHEN THE NEURON ADAPTS

We assess and compare the performance of each learning rule on a simple spatio-temporal receptive field development task, with $N = 100$ presynaptic neurons converging onto a single postsynaptic cell (**Figure 2A**).

For each presynaptic neuron, a 5-s input spike train is generated once and for all (see Materials and Methods). All presynaptic spike trains are then replayed continuously 5,000 times. All synapses undergo STDP according to one of the three learning rules. Synaptic weights are all initially set to 1 mV, which yields an initial output firing rate of about 7.5 Hz. We set the target firing rate ρ_{target} of each learning rule such that the output firing rate stays very close to 7.5 Hz. To gather enough statistics, the whole experiment is repeated 10 times independently, each time with different input patterns. All results are therefore reported as mean and standard error of the mean (SEM) over the 10 trials.

All three learning rules developed very similar bimodal distributions of synaptic efficacies (**Figure 4A**), irrespective of the presence or absence of SFA. This is a well known consequence of additive STDP with hard bounds imposed on the synaptic weights (Kempster et al., 1999; Song et al., 2000). The firing rate stabilizes at 7.5 Hz as desired, for all plasticity rules (not shown). In **Figure 4B**, we show the evolution of the MI (solid lines) as a function of learning time. It is computed as described in Section “Materials and Methods,” from the postsynaptic activity gathered during 100 periods (500 s). Since we are interested in quantifying the ability of different learning rules to enhance information transmission, we look at the information gain [defined as $MI(\alpha = 1) - MI(\alpha = 0)$] rather than the absolute value of the MI after learning. The triplet model reaches 98% of the “optimal” information gain while the pair model reaches 86% of it. Note that we call “optimal” what comes from the optimality model, but it is not necessarily the optimum in the space of solutions, because (i) a stochastic gradient ascent may not always lead to the global maximum, (ii) Toyoizumi et al.'s (2005) optimal learning rule involves a couple of approximations that may result in a sub-optimal algorithm, and (iii) their learning rule does not specifically optimize information transmission for our periodic input scenario, but rather in a more general setting where input spike trains are drawn continuously from a fixed distribution (stationarity).

It is instructive to compare how much information is lost for each learning rule when the synaptic weights are shuffled. Shuffling means that the distribution stays exactly the same, while the detailed assignment of each w_i is randomized. The dashed lines in **Figure 4B** depict the MI under these shuffling conditions. Each point is obtained from averaging the MI over 10 different shuffled versions of the weights. The optimal and triplet model lose respectively 33 and 32% of their information gains, while the pair model loses only 23%. This means that the optimal and triplet learning rules make a better choice in terms of the detailed assignment of each synaptic weight. For the pair learning rule, a larger part of the information gain is a mere side-effect of the weight distribution becoming bimodal. As an aside, we observe that the MI is the same (4.5 bits) in the “shuffled” condition for all three learning rules. This is an indication that we can trust our information comparisons. The result is also compatible with the value found by randomly setting 20 weights to the maximum value and the others to 0 (**Figure 2B**, square mark).

How is adaptation involved in this increased channel capacity? In **Figure 2C**, the MI is plotted as a function of the postsynaptic firing rate, for an adaptive (black dots) and a non-adaptive (gray dots) neuron, irrespective of synaptic plasticity. Each point in the figure is obtained by setting randomly a given fraction χ of synaptic

weights to the upper bound (4 mV), and the rest to 0 mV. The weight distribution stays bimodal, which leaves the neuron in a high information transmission state. χ is varied in order to cover a wide range of firing rates. We see that adaptation enhances information transmission at low firing rates (<10 Hz). The MI has a maximum at 7.5 Hz when the neuron is adapting (black circles). If adaptation is removed, the peak broadens and shifts to about 15 Hz (green circles). If the energetic cost of firing spikes is also taken into account, the best performance is achieved at 3 Hz, whether adaptation is enabled or not. This is illustrated in **Figure 2C** (lower plot) where the information per spike is reported as a function of the firing rate.

Is adaptation beneficial in a general sense only, or does it differentially affect the three learning rules? To answer this question, we have the neuron learn again from the beginning, SFA being switched off. The temporal evolution of the MI for each learning rule is shown in **Figure 4C**. Overall, the MI is lower when the neuron does not adapt (compare **Figure 4B** and **Figure 4C**), which is in agreement with the previous paragraph and **Figure 2C**. Importantly, the triplet model loses its advantage over the pair model when adaptation is removed (compared red and blue lines in **Figure 4C**). This suggests a specific interaction between synaptic plasticity and the intrinsic postsynaptic dynamics in the optimal and triplet models. This is further investigated in later sections.

Finally, the main results of **Figure 4** also hold when the distribution of weights remains unimodal. To achieve unimodal distributions with STDP, the hypothesis of hard-bounded synaptic efficacies must be relaxed. We implemented a form of weight-dependence of the weight change, such that LTP stays independent of the synaptic efficacy, while stronger synapses are depressed more strongly (see Materials and Methods). The weight-dependent factor for LTD had traditionally been modeled as being directly proportional to w_j (e.g., van Rossum et al., 2000), which provides a good fit to the data obtained from cultured hippocampal neurons by Bi and Poo (1998). Morrison et al. (2007) proposed an alternative fit of the same data with a different form of weight-dependence of LTP. Here we use a further alternative (see Materials and Methods, and **Figure 5A**). We require that the multiplicative factors for LTP and LTD exactly match at $w_j = w_0 = 1$ mV, where initial weights are set in our simulations. Further, we found it necessary that the slope of the LTD modulation around w_0 be less than 1. Indeed, our neuron model is very noisy, such that reproducible pre–post pairs that need to be reinforced actually occur among a sea of random pre–post and post–pre pairs. If LTD too rapidly overcomes LTP above w_0 , there is no chance for the correlated pre–post spikes to evoke sustainable LTP. The slope must be small enough for correlations to be picked up. This motivates our choice of weight dependence for LTD as depicted in **Figure 5A**. The weight distributions for all three learning rules stay indeed unimodal, but highly positively skewed, such that the neuron can really “learn” by giving some relevant synapses large weights (tails of the distributions in **Figure 5A**). Note that the obtained weight distributions resemble those recorded by Sjöström et al. (2001) (see e.g., **Figure 3C** in their paper).

The evolution of the MI along learning time is reported in **Figure 5C**. Overall, MI values are lower than those of **Figure 4B**. Unimodal distributions of synaptic efficacies are less informative than purely bimodal distributions, reflecting the lower degree of

specialization to input features. Such distributions may however be advantageous in a memory storage task where old memories which are not recalled often need to be erased to store new ones. In this scenario, strong weights which become irrelevant can quickly be sent back from the tail to the main weight pool around 1 mV. For a detailed study of the impact of the weight-dependence on memory retention, see Billings and van Rossum (2009).

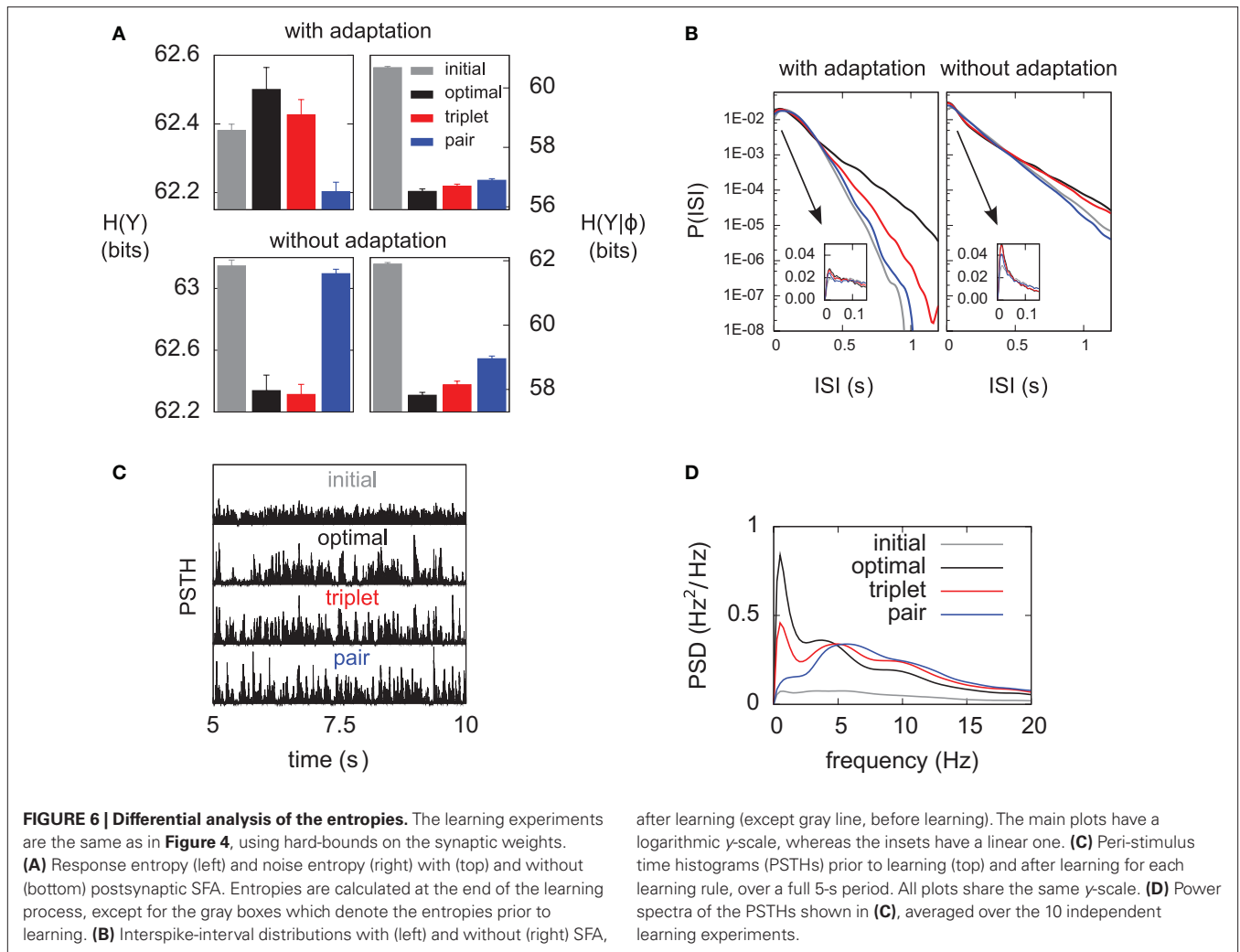
We see that it is difficult to directly compare absolute values of the MI in **Figure 5C**, since the “shuffled” MIs (dashed lines) do not converge to the same value. This is because some weight distributions are more skewed than others (compare red and blue distributions in **Figure 5A**). In the present study, we are more interested in knowing how good plasticity rules are at selecting individual weights for up- or down-regulation, on the basis of the input structure. We would like our performance measure to be free of the actual weight distribution, which is mainly shaped by the weight-dependence of Eq. 23. We therefore compare the normalized information gain, i.e., $[\text{MI}(\alpha = 1) - \text{MI}(\alpha = 0)] / [\text{MI}_{\text{sh}}(\alpha = 1) - \text{MI}(\alpha = 0)]$, where MI_{sh} denotes the MI for shuffled weights. The result is shown in **Figure 5D**: the triplet is again better than the pair model, provided the postsynaptic neuron adapts.

Our simulations show that when SFA modulates the postsynaptic firing rate, the triplet model yields a better gain in information transmission than pair-STDP does. When adaptation is removed, this advantage vanishes. There must be a specific interaction between triplet-STDP and adaptation that we now seek to unravel.

TRIPLET-STDP INCREASES THE RESPONSE ENTROPY WHEN THE NEURON ADAPTS

Information transmission improves if the neuron learns to produce more diverse spike trains [$H(\mathbf{Y}^k)$ increases], and if the neuron becomes more reliable [$H(\mathbf{Y}^k|\phi)$ decreases]. In **Figure 6A** we perform a differential analysis of both entropies, on the same data as presented in **Figure 4** (i.e., for hard-bounded STDP). Whether the postsynaptic neuron adapts (top) or not (bottom), the noise entropy (right) is drastically reduced, and the triplet learning rule does so better than the pair model (compare red and blue). The differential impact of adaptation on the two models can only be seen in the behavior of the response entropy $H(\mathbf{Y}^k)$ (left). When the postsynaptic neuron adapts, triplet- and optimal STDP both increase the response entropy, while it decreases with the pair model. This behavior is reflected in the interspike-interval (ISI) distributions, shown in **Figure 6B**. With adaptation, the optimal and triplet rules produce distributions that are close to an exponential (which would be a straight line in the logarithmic γ -scale). In contrast, the ISI distribution obtained from pair-STDP stays almost flat for ISIs between 25 and 120 ms. Without adaptation, the optimal and triplet models further sparsifies the ISI distribution which then becomes sparser than an exponential, reducing the response entropy.

Qualitative similarities between the optimal and triplet models can also be found in the power spectrum of the peri-stimulus time histogram (PSTH). The PSTHs are plotted in **Figure 6C** over a full 5-s period, and their average power spectra are displayed in **Figure 6D**. The PSTH is almost flat prior to learning, reflecting the absence of feature selection in the input. Learning in all three learning rules creates sharp peaks in the PSTH, which illustrates the drop



in noise entropy seen in **Figure 6A** (right). The pair learning rule produces PSTHs with almost no power at low frequencies (below 5 Hz). In contrast, these low frequencies are strongly boosted by the optimal and triplet models. This is however not specific to SFA being on or off (not shown). We give an intuitive account for this in Section “Discussion.”

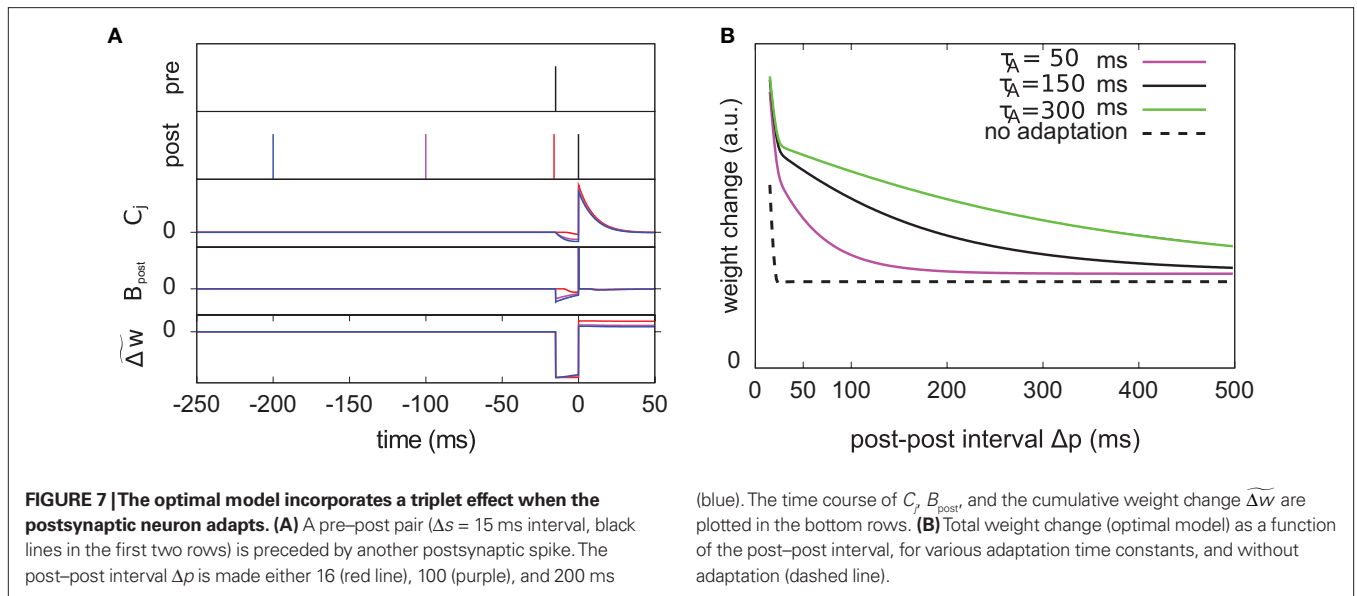
This section has shed light on qualitative similarities in the way the optimal and triplet learning rules enhance information transmission in an adaptive neuron. We now seek to understand the reason why taking account of triplets of spikes would be close-to-optimal in the presence of postsynaptic SFA.

THE OPTIMAL MODEL EXHIBITS A TRIPLET EFFECT

How similar is the optimal model to the triplet learning rule? In essence, the optimal model is a stochastic gradient learning rule, which updates the synaptic weights at every time step depending on the recent input–output correlations and the current relevance of the postsynaptic state. In contrast to this, phenomenological models require changing the synaptic efficacy upon spike occurrence only. It is difficult to compress what happens between spikes in the optimal model down to a single weight change at spike times. However we know that the dependence of LTP on previous postsynaptic

firing is a hallmark of the triplet rule, and is absent in the pair rule. We therefore investigate the behavior of the optimal learning rule on post–pre–post triplets of spikes, and find a clear triplet effect (**Figure 7**).

We consider an isolated post–pre–post triplet of spikes, in this order (**Figure 7A**). Isolated means that the last pre- and postsynaptic spikes occurred a very long time before this triplet. Let t_{post}^1 , t_{pre} , and t_{post}^2 denote the spike times. The pre–post interval is kept constant equal to $\Delta s = t_{post}^2 - t_{pre} = 15$ ms. We vary the length of the post–post interval $\Delta p = t_{post}^2 - t_{post}^1$ from 16 to 500 ms. The resulting weight change is depicted in **Figure 7B**. For comparison, the triplet model would produce – by construction – a decaying exponential with time constant τ_y . In the optimal model, potentiation decreases as the post–post interval increases. Two times constants show up in this decay, which reflect that of refractoriness (2 ms) and adaptation (150 ms). The same curve is drawn for two other adaptation time constants (see red and blue curves). When adaptation is removed, the triplet effect vanishes (dashed curve). It should be noted that the isolated pre–post pair itself (i.e., large post–post interval) results in a baseline amount of LTP, which is not the case in the triplet model. **Figure 7A** shows how this effect arises mechanistically. Three different triplets



are shown, with the pre–post pair being fixed, and the post–post interval being either 16, 100, or 200 ms (red, purple, and blue respectively).

To further highlight the similarity between the optimal learning rule and the triplet model, we now derive an analytical expression for the optimal weight change that follows a post–pre–post triplet of spikes. Let us observe that the final cumulated weight change evoked by the triplet is dominated by the jump that occurs just following the second postsynaptic spike (**Figure 7A**) – except for the negative jump of size λ that follows the presynaptic spike arrival, but this is a constant. Our analysis therefore concentrates on the values of $C_j(t_{\text{post}}^2)$ and $B_{\text{post}}(t_{\text{post}}^2)$. Let us denote by $\epsilon_j = \exp(-\Delta s/\tau_m)$ the value of the unitary synaptic PSP at time t_{post}^2 . Around the baseline potential $u_b = 19$ mV, the gain function is approximately linear (cf. **Figure 1A**), i.e., $g(u_b + w_j \epsilon_j) \approx g_b + g'_b w_j \epsilon_j$ where $g_b = g(u_b)$ and $g'_b = dg/du|_{u_b}$ are constants. From Eq. 14, we read $B_{\text{post}}(t_{\text{post}}^2) = \log[1 + (g'_b w_j \epsilon_j / g_b)] \delta(0)$, which is approximately equal to

$$B_{\text{post}}(t_{\text{post}}^2) \approx \frac{g'_b}{g_b} w_j \epsilon_j \delta(0) \quad (24)$$

assuming the contribution of $w_j \epsilon_j$ is small compared to the baseline gain g_b . The term proportional to M in Eq. 14 is negligible compared to the δ -function. From Eq. 13, we see that

$$C_j(t_{\text{post}}^2) = \frac{\epsilon_j g'_b}{g_b + g'_b w_j \epsilon_j} + C_j(t_{\text{post}}^2 - \epsilon) \quad (25)$$

The total weight change following the second postsynaptic spike is therefore

$$\Delta w_j(t_{\text{post}}^2) \approx \left(\frac{g'_b}{g_b} \right)^2 w_j \epsilon_j^2 + \frac{g'_b}{g_b} w_j \epsilon_j C_j(t_{\text{post}}^2 - \epsilon) \quad (26)$$

where

$$C_j(t_{\text{post}}^2 - \epsilon) = - \int_{t_{\text{pre}}}^{t_{\text{post}}^2 - \epsilon} \exp\left(-\frac{t_{\text{post}}^2 - t}{\tau_c}\right) \exp\left(-\frac{t - t_{\text{pre}}}{\tau_m}\right) g'_b M(t) dt \quad (27)$$

Since we have taken $\tau_c = \tau_m$, the first two exponentials collapse into ϵ_j . To carry out the integration, let us further simplify the adaptation model into $M(t) = 1 - \exp(-(t - t_{\text{post}}^1)/\tau_A)$, assuming that $t_{\text{pre}} - t_{\text{post}}^1 > 2$ ms so that the refractoriness has already vanished at the time of the presynaptic spike, while adaptation remains. It is also assumed that the triplet is isolated, so that we can neglect the cumulative effect of adaptation. Eq. 27 becomes

$$C_j(t_{\text{post}}^2 - \epsilon) = -g'_b \epsilon_j \left[\Delta s + \tau_A \exp\left(-\frac{\Delta p}{\tau_A}\right) \left(1 - \exp\left(\frac{\Delta s}{\tau_A}\right)\right) \right] \quad (28)$$

If $\Delta s \ll \tau_A$, the last term into square brackets is approximately $\Delta s/\tau_A$. If not, ϵ_j becomes so small that the whole r.h.s of Eq. 26 vanishes. To sum up, the total weight change following the second postsynaptic spike is given by

$$\Delta w_j(t_{\text{post}}^2) = \frac{g_b'^2}{g_b} w_j \epsilon_j^2 \left(\frac{1}{g_b} - \Delta s \right) + \frac{g_b'^2}{g_b} \Delta s w_j \epsilon_j^2 \exp\left(-\frac{\Delta p}{\tau_A}\right) \quad (29)$$

The first term on the r.h.s of Eq. 29 is a pair term, i.e., a weight change that depends only on the pre–post interval Δs . We note that it is proportional to ϵ_j^2 , meaning that the time constant of the causal part of the STDP learning window is half the membrane time constant. The second term exactly matches the triplet model, when $\tau_A = \tau_y$ and $\tau_+ = \tau_m/2$. Indeed, the triplet model would yield the following weight change:

$$\Delta w_j^{\text{triplet}}(t_{\text{post}}^2) \approx A_3^+ \epsilon_j \exp\left(-\frac{\Delta p}{\tau_y}\right) \quad (30)$$

From this we conclude that the triplet effect, which primarily arose from phenomenological minimal modeling of experimental data, also emerges from an optimal learning rule when the postsynaptic neuron adapts. To understand in more intuitive terms how the triplet mechanism relates to optimal information transmission, let us consider the case where the postsynaptic neuron is fully deterministic. If so, the noise entropy is null, so that maximizing

information transfer means producing output spike trains with maximum entropy. If the mean firing rate ρ_{targ} is a further constraint, output spike trains should be Poisson processes, which as a by-product would produce exponentially distributed ISIs. If the neuron is endowed with refractory and adapting mechanisms, there is a natural tendency for short ISIs to appear rarely. Therefore, plasticity has to fight against adaptation and refractoriness to bind more and more stimulus features to short ISIs. The triplet effect is precisely what is needed to achieve this: if a presynaptic spike is found to be responsible for a short ISI, it should be reinforced more than if the ISI was longer. This issue is further developed in Section “Discussion.”

OPTIMAL STDP IS TARGET-CELL SPECIFIC

The results of the previous sections suggest that STDP may optimally interact with adaptation to enhance the channel capacity. In principle, if STDP is optimized for information transmission, it cannot ignore the intrinsic dynamics of the postsynaptic cell which influences the mapping between input and output spikes. The cortex is known to exhibit a rich diversity of cell types, with the corresponding range of intrinsic dynamics, and in parallel, STDP is target-cell specific (Tzounopoulos et al., 2004; Lu et al., 2007). Within the optimality framework, we should therefore be able to predict this target-cell specificity of STDP by investigating the predictions of the optimal model in the context of *in vitro* pairing experiments. Predictions should be made for different types of postsynaptic neurons, and be compared to experimental data. The optimal learning rule was shown in Toyoizumi et al. (2007) to share some features with STDP. We here extend this work to a couple of additional features including the frequency dependence. We also apply it to another type of postsynaptic cell, an inhibitory FS interneuron, for which *in vitro* data exist.

Only one synapse is investigated, with unit weight $w_0 = 1$ mV before the start of the experiment. Sixty pre–post pairs with given interspike time Δs are repeated in time with frequency f . The subsequent weight change given by Eq. 12 is reported as a function of both parameters (**Figures 8A,B**).

The optimal model features asymmetric timing windows at 1, 20, and 50 Hz pairing frequencies (**Figure 8A**). At 1 and 20 Hz, pre-before-post yields LTP and post-before-pre leads to LTD. At 50 Hz the whole curve is shifted upwards, resulting in LTP on both sides. The model qualitatively agrees with the experimental data reported in Sjöström et al. (2001), redrawn for comparison (**Figure 8A**, circles).

The frequency dependence experimentally found in Markram et al. (1997) and Sjöström et al. (2001) is also qualitatively reproduced (**Figure 8B**). Post–pre pairing ($\Delta s = -10$ ms, green curve) switches from LTD at low frequency to LTP at higher frequencies, which is consistent with the timing windows in **Figure 8A**. For pre–post pairing ($\Delta s = +10$ ms, blue curve), LTP also increases with the pairing frequency. We also found that when SFA was removed, it was impossible to have a good fit for both the time window and the frequency dependence (not shown).

To further elucidate the link between optimal STDP and the after-spike kernel ($g_R + g_A$ in Eq. 5), we ask whether plasticity at excitatory synapses onto FS interneurons can be accounted for in the same principled manner. In general, the intrinsic dynamics of

inhibitory interneurons are very different from that of principal cells in cortex. STDP at synapses onto those cells is also different from STDP at excitatory-to-excitatory synapses (Tzounopoulos et al., 2004; Lu et al., 2007). The dynamics of FS cells are well modeled using a kernel which is shown in **Figure 8D** (Mensi et al., 2010). We augment the after-spike kernel with an additional variable g_B governed by

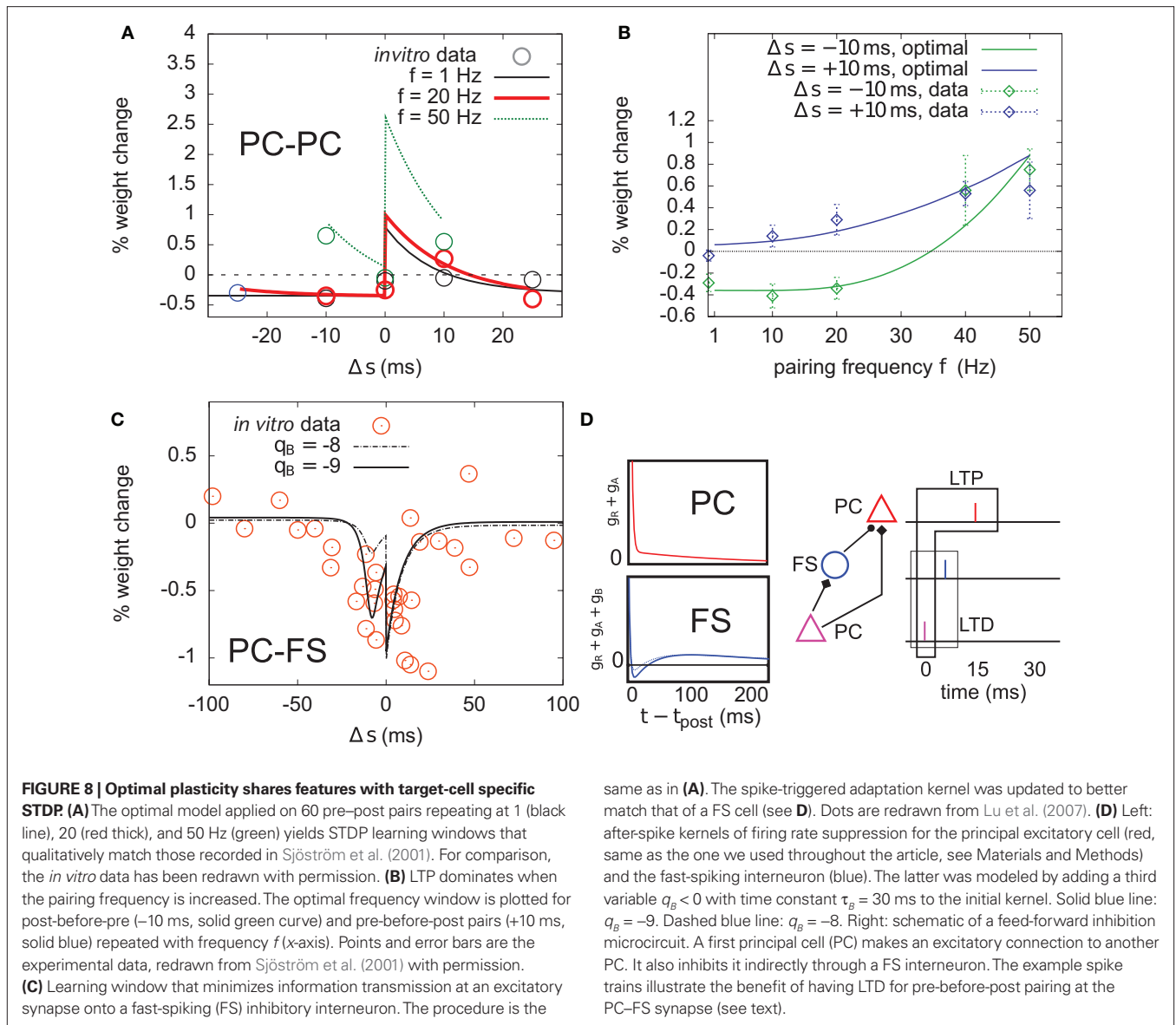
$$\frac{dg_B}{dt} = -\frac{g_B}{\tau_B} + q_B Y(t) \quad (31)$$

Parameters were set to $\tau_B = 30$ ms, $\tau_A = 150$ ms, $q_B = -9$, and $q_A = 4$. The resulting kernel (i.e., $g_R + g_A + g_B$ – **Figure 8D**, blue kernel) exhibits after-spike refractoriness followed by a short facilitating period before adaptation takes over (note that the kernel is suppressive, meaning that positive values correspond to suppression of activity while negative values mean facilitation). Since interneurons do not project over long distances to other areas, the infomax objective function might not appear as well justified. Instead, let us consider the simple microcircuit shown in **Figure 8D**. A first principal cell (PC) makes an excitatory synapse onto a second PC, and we assume the infomax principle is at work. The first PC inhibits the second PC via a FS interneuron. How, intuitively, should the PC-to-FS synapse change so that the FS cell also contributes to the overall information maximization between the two PCs? In a very crude understanding of the infomax principle, if a pre-before-post pair of spikes is evoked at the PC–PC synapse (see spike trains in **Figure 8D**), the probability of having this pair again should be increased. If a similar pre-before-post pair is simultaneously evoked at the PC–FS synapse, then decreasing its weight will make it less likely that the FS spike again after the first PC. This in turn makes it more likely that the first PC–PC pair of spike will occur again. Therefore, PC–FS synapses should undergo some sort of anti-Hebbian learning. In fact, we found information minimization (i.e., the optimal model with opposite learning rate) to yield a good match between the simulated STDP time window (**Figure 8C**) and that found in Lu et al. (2007), which also exhibits LTD on both sides with some LTP at large intervals (see orange dots, superimposed). The post-before-pre part of the window can be understood intuitively: when a presynaptic spike arrives a few milliseconds after a postsynaptic spike, it falls in the period where postsynaptic firing is facilitated ($q_B < 0$). Therefore, it still has some influence on the subsequent postsynaptic activity. In order to avoid later causal pre–post events, the weight should be decreased. We see that the optimal STDP window depends on the after-spike kernel that describes the dynamical properties of the postsynaptic cell: q_B directly modulates the post–pre part of the window (see dashed curve in **Figure 8C**).

Together, these results suggest that if STDP is considered as arising from an optimality principle, it naturally interacts with the dynamics of the postsynaptic cell. This might underlie the target-cell specificity of STDP (Tzounopoulos et al., 2004; Lu et al., 2007).

DISCUSSION

Experiments (Markram et al., 1997; Sjöström et al., 2001; Froemke et al., 2006) as well as phenomenological models of STDP (Senn et al., 2001; Froemke et al., 2006; Pfister and



Gerstner, 2006; Clopath et al., 2010) point to the fact that LTP is not accurately described by independent contributions from neighboring postsynaptic spikes. In order to reproduce the results of recent STDP experiments, at least two postsynaptic spikes must interact in the LTP process. We have shown that this key feature (“triplet effect” in Pfister and Gerstner, 2006; Clopath et al., 2010; and similarly in Senn et al., 2001) happens to be optimal for an adapting neuron to learn to maximize information transmission. We have compared the performance of an optimal model (Toyoizumi et al., 2005) to that of two minimal STDP models. One of them incorporated the triplet effect (Pfister and Gerstner, 2006), while the second one did not (standard pair-based learning rule; Gerstner et al., 1996; Kempter et al., 1999; Song et al., 2000). The triplet-based model performs very close to the optimal one, and this advantage over pair-STDP disappears when SFA is removed from the intrinsic dynamics of the postsynaptic cell.

Our results are not restricted to additive STDP in which the amount of weight change is independent of the weight itself. It also holds when the amount of LTD increases with the efficacy of the synapse, a form which better reflects experimental observations (Bi and Poo, 1998; Sjöström et al., 2001). In the model introduced here, the amount of LTD is modulated by a sub-linear function of the synaptic weight. The deviation from linearity is set by a single parameter $a > 0$, with the purely multiplicative dependence of van Rossum et al. (2000) being recovered when $a = 0$. Since we modeled only a fraction of the total input synapses, we assumed a certain level of noise in the postsynaptic cell to account for the activity of the remaining synapses, thereby staying consistent with the framework of information theory in which communication channels are generally considered noisy. Because of this noise level, we found a large a was required for the weight distribution to become positively skewed as reported by Sjöström et al. (2001) (cortex layer V). For both the pair and triplet learning rules, the noisier the postsynaptic

neuron, the weaker the LTD weight-dependence (i.e., the larger a) must be to keep a significant spread of the weight distribution. This means that other (possibly simpler) forms of weight dependence for LTD would work equally well, provided the noise level is adjusted accordingly. For example, in a nearly deterministic neuron, input–output correlations are strong enough for the weight-distribution to spread even when LTD depends linearly on the synaptic weight ($a = 0$, not shown).

In the original papers where the optimal and triplet rule were first described, it was pointed out that both rules could be mapped onto the BCM learning rule (Bienenstock et al., 1982). Both learning rules are quadratic in the postsynaptic activity. In turn, the link between the BCM rule and ICA has also already been researched (Intrator and Cooper, 1992; Blais et al., 1998; Clopath et al., 2010), as has the relationship between the infomax principle and ICA (Bell and Sejnowski, 1995). It therefore does not come as a surprise that the triplet model performs close to the infomax optimal learning rule. What is novel is the link to adaptation and spike after-potential.

We have also shown that when the optimal or triplet plasticity models are at work, the postsynaptic neuron learns to transmit information in a wider frequency band (**Figure 6D**): both rules evoke postsynaptic responses that have substantial power below 5 Hz, in contrast to the pair-based STDP rule. This is intuitively understood from the triplet effect combined with adaptation. Let us imagine STDP starts creating a peak in the PSTH so that we have, with high probability, a first postsynaptic spike at time t_0 . If a presynaptic spike at time $t_0 + (\Delta/2)$ is followed by a further postsynaptic spike at time $t_0 + \Delta$ (Δ on the order of 10 ms), the triplet effect reinforces the connection from this presynaptic unit. In turn, it will create another peak at time $t_0 + \Delta$, and this process can continue. Peaks thus extend and become broader, until adaptation becomes strong enough to prevent further immediate firing. The next series of peaks will then be delayed by a few hundred milliseconds. Broadening of peak widths and ISIs together introduce more power at lower frequencies in the PSTH.

One should bear in mind that neurons process incoming signals in order to convey them to other receivers. Although the information content of the output spike train really is an important quantity with respect to information processing, the way it can be decoded by downstream neurons should also be taken into account. Some “words” in the output spike train may be more suited for subsequent transmission than others. It has been suggested (Lisman, 1997) that since cortical synapses are intrinsically unreliable, isolated incoming spikes cannot be received properly, whereas bursts of action potentials evoke a reliable response in the receiving neuron. There is a lot of evidence for burst firing in many sensory systems (see Krahe and Gabbiani, 2004 for a review). As shown in **Figure 6**, the optimal and triplet STDP models tend to sparsify the distribution of ISIs, meaning that the neuron learns to respond vigorously (very short ISIs) to a larger number of features in the input stream, while remaining silent for longer portions of the stimulus. The neuron thus overcomes the effects of adaptation, which in baseline conditions (before learning) gives the ISI distribution a broad peak and a Gaussian-like drop-off. Our results therefore suggest that reliable occurrence of short ISIs can arise from STDP in adaptive neurons that are not intrinsic bursters. This is in line with Eyherabide et al.

(2008), which recently provided evidence for high information transmission through burst activity in an insect auditory system (*Locusta migratoria*). The recorded neurons encoded almost half of the total transmitted information in bursts, and this was also shown not to require intrinsic burst dynamics.

Since our results rely on the outcome of a couple of numerical experiments, one might be concerned about the validity of the findings outside the range of parameter values we have used. There are for example a couple of free parameters in the neuron model. It is obviously difficult to browse the full high-dimensional parameter space and search for regions where the results would break down. We therefore tried to constrain our neuron parameters in a sensible manner. For example, the parameters of the SFA mechanism (q_A and τ_A) were chosen such that the response properties to a step in input firing rate would look plausible (**Figure 1C**). The noise parameter r_0 and the threshold value u_T were chosen so as to achieve an output rate of 7.5 Hz when all synaptic weights are at 1 mV. We acknowledge, though, that r_0 could be made arbitrarily large (reducing the amount of noise) since u_T can compensate for it. In the limit of very low noise, information transmission cannot be improved by increasing the neuron’s reliability anymore, since the noise entropy would already be minimal. We have shown however that a substantial part of the information gain found in the optimal and triplet models are due to an increased response entropy. This qualitative similarity, together with the structural similarities highlighted in **Figures 7 and 8**, lead us to believe that our results would still hold in the deterministic limit, and for noise levels in between. The optimal plasticity rule becoming ill-defined in this limit, we did not investigate this further.

To what extent can we extrapolate our results to the optimality of synaptic plasticity in the real brain? It obviously depends on the amount of trust one can put into this triplet model. Phenomenological models of STDP are usually constructed based on the results of *in vitro* experiments. They end up reproducing the quantitative outcome of only a few pre–post pairing schemes which are far from spanning the full complexity of real spike trains. To what extent can these models be trusted in more natural situations? From a machine learning perspective, a minimal model is likely to generalize better than a more detailed model, because its small number of free parameters might prevent it from overfitting the experimental data at the expense of its interpolation/extrapolation power. In this study, we have put the emphasis on an extrapolation of recent minimal models (Pfister and Gerstner, 2006; Clopath et al., 2010): the amount of LTP obtained from a pre-before-post pair increases with the recent postsynaptic firing frequency. By construction, the models account for the frequency dependence of the classical pairing experiment (they are fitted on this, among other things). However, they are seriously challenged by a more detailed study of spike interactions at L2/3 pyramidal cells (Froemke et al., 2006). There, it was explicitly shown that (n -posts)–pre–post bursts yield an amount of LTD which grows with n , the number of postsynaptic spikes in the burst preceding the pair. In contrast, post–pre–post triplets in hippocampal slices lead to LTP in a way that is consistent with the triplet model (Wang et al., 2005). The results of our study should therefore be interpreted bearing in mind the variability in experimental results. The recurrent *in vitro* versus *in vivo* debate should also be considered: synaptic

plasticity depends on a lot of biochemical parameters for which the slice conditions do not faithfully reflect the normal operating mode of the brain.

A second controversy lies in our optimality model itself. While efficient coding of presynaptic spike trains may seem a reasonable goal to achieve at, say, thalamocortical synapses in sensory cortices, many other objectives could well be considered when it comes to other brain areas. Some examples are optimal decision making through risk balancing, reinforcement learning via reward maximization, or optimal memory storage and recall in autoassociative memories. It will be interesting to see more STDP learning rules in functionally different areas and how these relate to optimality principles.

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